

# FULLY SECURE MESSAGE TRANSMISSION OVER NON-SECURE CHANNELS WITHOUT CRYPTOGRAPHIC KEY EXCHANGE

## BACKGROUND OF THE INVENTION

### 1. Field of the Invention

The present invention relates generally to cryptography and, more particularly, to the secure transmission of messages between parties using non-secure communication channels.

### 2. Description of the Prior Art

Cryptographic systems are widely used to ensure the privacy of messages communicated over insecure channels. Such systems prevent the extraction of information by unauthorized parties from messages transmitted over insecure channels, thus assuring the sender that a transmitted message is being read only by the intended recipient.

Two distinct classes of cryptographic methods and protocols are widely used, symmetric-key cryptography and public-key cryptography. In symmetric-key techniques, the same key and cryptographic method are used by both the encoding party for sending the message and by the receiving party for decoding the message. The security of symmetric-key protocols is based on the secrecy of the required key and the strength of the cryptographic method. The message can be properly decoded by the receiving party only if the transmitting party and the receiving party possess the identical key used for encoding the message.

For conventional public-key key techniques such as those pioneered by Diffie and Hellman, there are two keys, a public key to which anyone can gain access and with which a plaintext message is encrypted, and a private key that only the recipient possesses and with which the encrypted message is decrypted. The security of public key protocols relies on the considerable difficulty of determining the private key by analyzing the public key. Such computational difficulty is essentially inherent in most public key processes making them considerably slower than symmetric-key protocols even for the recipient who possesses the private key. Chang has devised protocols for the exchange (or simultaneous creation) of cryptographic keys similar to the broadcast-and-response processes of public-key techniques. These key exchange techniques appear to be fully secure but simply create cryptographic keys for subsequent use by other cryptographic systems; they do not allow for the direct transmission of agent-created messages.

Mechanical systems exist which are analogous to symmetric-key and public-key systems. For the symmetrical-key process, the mechanical analogy is a locked box carried between the two parties where each party has previously obtained a copy of the key that opens the box. The first, transmitting party unlocks and opens the box, places the message inside, relocks the box and sends it to the second, receiving party who then unlocks the box and

1 removes the message. The public-key process resembles an unlocked box and open lock  
2 with a special locking-only key left in a public place. The locking-only key is available  
3 for public inspection and analysis. Any interested, transmitting party may place a  
4 message in the box, close the lock, and secure the lock with the locking-only key; only  
5 the box's recipient owner will be able to unlock the lock with a different unlocking-only  
6 key, open the box, and remove the message.

7  
8 A third mechanical analogy demonstrates the processes of the claimed invention. In it, a  
9 first party places a message in a box, locks it, and sends it to the intended recipient. The  
10 recipient places a second lock on the box and returns it to the original sender. The first  
11 party then removes the first lock from the doubly locked box and sends the still singly  
12 locked box to the intended recipient a final time. The recipient then removes the second  
13 lock, opens the box, and retrieves the message. This is the essence of the so-called three-  
14 pass protocol. Neither party shares a key to the box, differentiating this process from the  
15 symmetric-key process, and the keys to the box are never available for public inspection  
16 and analysis, differentiating this process from the public-key processes. This three-pass  
17 protocol as utilized in the claimed invention represents a third distinct class of encryption  
18 techniques that could best be described as independent-key processes, since neither party  
19 possesses nor shares a key with the other party.

20  
21 In the context of modern cryptography, Schneier describes the three-pass process as a  
22 public-key system and attributes the protocol to Shamir. A primary limitation of the  
23 three-pass protocol has been the ability of an eavesdropping third party to use the three  
24 transmitted encrypted messages to "crack the code" and derive the original plaintext  
25 message. Schneier demonstrates that even otherwise secure symmetric key protocols  
26 such as one-time pads are not secure in a three-pass process. Shamir (concurrently with  
27 Omura) devised an encryption algorithm for the three-pass protocol using an RSA-like  
28 factoring algorithm as the key mechanism. Others have used the three-pass protocol as  
29 well; for example, Massey devised a key mechanism based on  $GF(2^m)$  finite fields. Both  
30 implementations use key processes that are computationally difficult – like conventional  
31 public-key methods – but not fully secure.

32  
33 The claimed invention uses the three-pass protocol and creates cryptographic processes  
34 that are fully secure while requiring no cryptographic key exchange. The processes of  
35 the invention are differentiated from the previous, public-key-like, three-pass protocols.  
36 The technique of the invention is designated as an independent-key process.

## 37 38 39 SUMMARY AND OBJECTS OF THE INVENTION

40  
41 One object of the invention is to provide a fully secure cryptographic technique for  
42 maintaining privacy of messages conveyed or transmitted over non-secure channels while  
43 requiring no exchange of any cryptographic keys, either public or private.  
44

1 Accordingly, it is another object of this invention to allow two parties to the  
2 communication of a message to exchange the message privately even though another  
3 party (an eavesdropper) intercepts all of their communications.

4  
5 Another object of this invention is to provide for the fully secure exchange of messages –  
6 including cryptographic keys – between two parties even when the communication is  
7 transmitted over non-secure channels.

8  
9 Another object of this invention is to provide for a message exchange protocol that is  
10 fully secure against all but a brute force cryptanalysis attack.

11  
12 Another object of this invention is to provide for a fully secure message exchange  
13 protocol that is faster than most; if not all, present protocols that do not require each party  
14 to share identical encryption/decryption keys.

15  
16 Briefly, for two parties desiring the private communication of a plaintext message (P) –  
17 the first, transmitting party (T) and the second, receiving party (R) – three encrypted  
18 messages ( $C_1$ ,  $C_2$ , and  $C_3$ ) are created and communicated between the parties to generate  
19 the fully secure transmission of the initial message P.

20  
21 The first party T chooses two distinct transformation processes ( $\alpha$  and  $\beta$ ) and key  
22 elements for those processes with characteristics such that the plaintext message P may  
23 be embodied in the output of the transformation process  $\alpha$ , the transformation process  $\beta$   
24 can be readily reversed, and the composite transformation of the operation of the  
25 transformation process  $\beta$  on the output of the process  $\alpha$  embodying message P cannot be  
26 reversed. The first encrypted message  $C_1$  is created as the output of the operation of the  
27 transformation process  $\beta$  on the output of the process  $\alpha$  embodying P and is transmitted  
28 by the first party T over a non-secure channel to the second party R.

29 The steps taken by the first party T in creating the first encrypted message  $C_1$  are  
30 represented as follows:

31		
32	$\alpha(P)$	The result of the transformation $\alpha$ embodies P
33	$\beta'$ exists	The transformation $\beta$ can be reversed where $\beta'$
34		represents the reverse transformation of $\beta$
35	$\beta(\alpha(P))'$ does not exist	The composite process of the transformation $\beta$
36		acted on the transformation $\alpha$ can not be reversed
37	$C_1 \Leftarrow \beta(\alpha(P))$	The encrypted message $C_1$ is assigned the
38		composite result of the transformation $\beta$ acted
39		on the transformation $\alpha$
40		

41 Reversal of a transformation is taken to mean that given the specific characteristics of the  
42 transformation and a specific output of that transformation, the corresponding inputs to  
43 the transformation can be derived. Transformations that cannot be reversed are those for  
44 which even when given the specific characteristics of the transformation and a specific  
45 output of that transformation, the corresponding inputs to the transformation cannot be  
46 derived. For the purpose of the invention, transformations may include but are not

limited to mathematical functions and their equivalents. For transformations consisting of mathematical functions, the process of reversing the transformations is known as inverting the functions. In general, the transformations referenced herein may exhibit a more limited or more expansive set of properties than those distinctly attributed to mathematical functions.

Upon receipt of the first encrypted message  $C_1$ , the second party R chooses a distinct transformation processes ( $\gamma$ ) and key elements for that process with characteristics such that the transformation process  $\gamma$  can be readily reversed and the composite transformation of the operation of the transformation process  $\gamma$  on the received encrypted message  $C_1$  cannot be reversed. The second encrypted message  $C_2$  is created as the output of the operation of the transformation process  $\gamma$  on the received encrypted message  $C_1$  and is transmitted by the second party R over a non-secure channel back to the first party T. The steps taken by the second party R in creating the second encrypted message  $C_2$  are represented as follows:

$\gamma'$ exists	The transformation $\gamma$ can be reversed where $\gamma'$ represents the reverse transformation of $\gamma$
$\gamma(C_1)'$ does not exist	The composite result of the transformation $\gamma$ acted on the first encrypted message $C_1$ cannot be reversed
$C_2 \leftarrow \gamma(C_1)$	The encrypted message $C_2$ is assigned the composite result of the transformation $\gamma$ acted on the first encrypted message $C_1$

Upon receipt of the second encrypted message  $C_2$ , the first party T reverses the second of the first two transformation processes  $\beta$  using the reversal process that is known to exist according to the initial choice of that transformation. The third and final encrypted message  $C_3$  is created as the output of the operation of the reverse transformation process  $\beta'$  on the received encrypted message  $C_2$  and is transmitted by the first party T over a non-secure channel back to the second party R. The steps taken by the first party T in creating the third encrypted message  $C_3$  are represented as follows:

$C_3 \leftarrow \beta'(C_2)$	The encrypted message $C_3$ is assigned the composite result of the reverse transformation $\beta'$ acted on the second encrypted message $C_2$
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Following the reversal transformation  $\beta'$ , the third encrypted message  $C_3$  represents the composite output of the operation of the transformation process  $\gamma$  on the output of the process  $\alpha$  embodying message P.

1 A key characteristic of the transformation processes  $\beta$  and  $\gamma$  for the protocol is the  
2 requirement of viable reverse transformations that are independent of the order of the  
3 reversal operations. That is, the composite result of the second encrypted message  $C_2$  is  
4 the culmination of all three transformation processes  $\alpha$ ,  $\beta$ , and  $\gamma$ , and it must be the case  
5 that the transformations  $\beta$  and  $\gamma$  can be reversed and applied to  $C_2$  – in any order – to  
6 yield the sole result of the first transformation  $\alpha$  alone. For mathematical functions, this  
7 condition is essentially equivalent to the commutative property. This key characteristic  
8 allows the operation of  $\beta$  on  $\alpha$  in creating  $C_1$  to be reversed as  $\beta'$  in the creation of  $C_3$   
9 even though the intervening transformation of  $\gamma$  has been applied. The invention  
10 identifies and applies transformations that make such order-independent reversal  
11 possible.

12  
13 Another constraint of the choice of the transformation process  $\gamma$  is that the composite  
14 transformation that is the result of the operation of the transformation process  $\gamma$  remaining  
15 in the output  $C_3$  after the reversal of  $\beta$  has been applied to  $C_2$  cannot be reversed.

16  
17 Upon receipt of the third encrypted message  $C_3$ , the second party R reverses the  
18 transformation processes  $\gamma$  using the reversal process that is known to exist according to  
19 the initial choice of that transformation. Following that reverse transformation, the result  
20 is simply the output of the process  $\alpha$  embodying message P. That is,

21  
22 
$$\alpha(P) \Leftarrow \gamma'(C_3),$$

23  
24 except that this copy of  $\alpha(P)$  is now in the possession of the second party R rather than in  
25 that of the initial party T. The second party R removes the plaintext message P from its  
26 embodiment in the output of the transformation process  $\alpha$  to yield possession of the  
27 original message created by T. The invention identifies and applies means of embodying  
28 the message P in the output of transformation process  $\alpha$  in a manner such that the second  
29 party R can remove the message P from that embodiment.

30  
31 The processes of the invention are distinctly different from previous implementations of  
32 three-pass protocols that used complex, public-key-like computational methods to  
33 implement the encryption components of each pass. The processes of the invention are  
34 straightforward transformation methods that are fully secure and yet computationally  
35 efficient. Because the invention doesn't require either party to possess or gain any  
36 information about the other's primary encryption process, the technique of the invention  
37 is designated as an independent-key process.

38  
39 An advantage of the present invention is that it is technically impossible for an  
40 eavesdropper, even knowing the transmitted quantities  $C_1$ ,  $C_2$ , and  $C_3$  and the general  
41 properties and processes of the transformations  $\alpha$ ,  $\beta$ , and  $\gamma$ , to directly determine the  
42 plaintext message P because no reverse transformations can be applied to the transmitted  
43 quantities to make that determination.

## BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a block diagram depicting a cryptographic system that may be employed for fully secure transmission of a message over non-secure channels without the prior exchange of cryptographic keys, according to the invention claimed herein.

Figure 2 is a block diagram depicting a general example of a possible embodiment of such a cryptographic system that may be employed for fully secure transmission of a message over non-secure channels without the prior exchange of cryptographic keys, according to the invention claimed herein.

Figure 3 is a block diagram depicting a specific example of a possible embodiment of such a cryptographic system that may be employed for fully secure transmission of a message over non-secure channels without the prior exchange of cryptographic keys, according to the invention claimed herein.

## DESCRIPTION OF THE PREFERRED EMBODIMENT

Referring to FIG. 1, a cryptographic system is shown in which all communication takes place over a non-secure channel 21. The non-secure channel 21 may include a telephone line, a radio connection, a cellular telephone connection, a fiber optic line, a microwave connection, a coaxial line, an infrared optical link, or any other communication technology that permits the transmission of information from a first location to a second location. Two-way communication is exchanged on the non-secure channel 21 between the initial converser 11 referred to as the transmitting party T and the second converser 31 referred to as the receiving party R using transceivers 22 and 23, for example digital cellular telephones, modems, or any other mechanism for converting information into the structure necessary for transmission by the non-secure channel 21. The transmitting party 11 possesses a plaintext message P 10 to be communicated to the receiving party 31.

Both the transmitting party T 11 and the receiving party R 31 use cryptographic devices 12 and 32 respectively, for encrypting and decrypting information under the action of the processes of this invention. Each cryptographic device 12 and 32 receives the output of transformation generators 13 and 33 respectively. The first transformation generator 13 creates the transformations  $\alpha$  14,  $\beta$  15 and  $\beta'$  16 which are provided to the cryptographic device 12. The transformation  $\beta'$  16 is the reverse transformation or inversion of process  $\beta$  15. The second transformation generator 33 creates the transformations  $\gamma$  34 and  $\gamma'$  35 which are provided to the cryptographic device 32. The transformation  $\gamma'$  35 is the reverse transformation of  $\gamma$  34.

The transmitting party T's 11 cryptographic device 12 encrypts the plaintext message P10 into the first cryptographic message  $C_1$  24 by transforming message P 10 through the transformations  $\alpha$  14 and  $\beta$  15 so that no reverse transformation is possible for the resulting output  $C_1$  24. The first cryptographic message  $C_1$  24 is then transmitted through

1 the first transceiver 22, over the non-secure channel 21, and through the second  
2 transceiver 23 to the receiving party R 31.

3  
4 The receiving party R's 31 cryptographic device 32 further encrypts the received first  
5 cryptographic message  $C_1$  24 into the second cryptographic message  $C_2$  25 by  
6 transforming  $C_1$  24 through the transformation  $\gamma$  34 so that no reverse transformation is  
7 possible for the resulting output  $C_2$  25. The second cryptographic message  $C_2$  25 is then  
8 transmitted through the second transceiver 23, back over the non-secure channel 21, and  
9 through the first transceiver 22 to the transmitting party T 11.

10  
11 The transmitting party T's 11 cryptographic device 12 partially decrypts the received  
12 second cryptographic message  $C_2$  25 into the third cryptographic message  $C_3$  26 by  
13 transforming  $C_2$  25 through the reverse transformation  $\beta'$  16 so that no reverse  
14 transformation is possible for the resulting output  $C_3$  26. The third cryptographic  
15 message  $C_3$  26 is then transmitted through the first transceiver 22, over the non-secure  
16 channel 21, and through the second transceiver 23 to the receiving party R 31.

17  
18 The receiving party R's 31 cryptographic device 32 device further decrypts the received  
19 third cryptographic message  $C_3$  26 by transforming  $C_3$  26 through the reverse  
20 transformation  $\gamma'$  35. The result now in the possession of the receiving party R 31 is the  
21 output of the process  $\alpha$  14 embodying P 10. The receiving party R 31 removes the  
22 plaintext message P 10 from its embodiment in the output of the transformation process  $\alpha$   
23 14 to yield possession of the original message created by T 11. The receiving party R 31  
24 does not know nor need to know the transmitting party T's 11 transformation process  $\beta$   
25 15 nor does the transmitting party T 11 know nor need to know the receiving party R's 31  
26 transformation process  $\gamma$  34. Both T 11 and R 31 know and utilize the transformation  
27 process  $\alpha$  14, but  $\alpha$  14 can be publicly known or transmitted from T 11 to R 31 without  
28 fear of interception, since the message P 10 cannot be decoded by an eavesdropper 41  
29 who knows only transformation process  $\alpha$  14. Because the invention doesn't require  
30 either party to possess or gain any information about the other's primary encryption  
31 processes, the technique of the invention is designated as an independent-key process.

32  
33 The cryptographic system of the invention includes a non-secure communications  
34 channel 21, making it possible for an eavesdropper 41 that is not included in the  
35 cryptographic system to receive all of the communications between the transmitting party  
36 T 11 and the receiving party R 31. The eavesdropper 41 may possess a cryptographic  
37 device 42 that includes the same processing capabilities and knowledge of the  
38 transformation processes as the cryptographic devices 12 and 32 available to the  
39 transmitting party T 11 and the receiving party R 31, and a transformation generator 43  
40 that includes the same capabilities and available transformation processes as the  
41 transformation generators 13 and 33 available to the transmitting party T 11 and the  
42 receiving party R 31. However, even given the full content of the encrypted messages  $C_1$   
43 24,  $C_2$  25, and  $C_3$  26, the eavesdropper 41 cannot directly determine or otherwise deduce  
44 the transformations  $\alpha$  14,  $\beta$  15, or  $\gamma$  34 to determine the original plaintext message P 10.  
45 The best that the eavesdropper 41 can do with the information from the messages  $C_1$  24,  
46  $C_2$  25, and  $C_3$  26 is to establish some limited relationships between some of the

1. components of the messages. However, knowledge of those relationships alone is not  
2 very informative or substantially useful to the eavesdropper 41 since the eavesdropper 41  
3 would still have to guess the values of many specific components of the transformations.  
4 Refining that relationship information would require an amount of effort by the  
5 eavesdropper 41 no less than that required for a brute-force break of the cryptographic  
6 system. Therefore, the cryptographic system is fully secure, being no more susceptible to  
7 cryptanalytic attack than to a brute-force attack

8  
9 As merely a general example of a possible embodiment of the processes of this invention,  
10 the basic techniques of matrix algebra may be applied to create transformations that  
11 satisfy the requirements of the invention. This example is demonstrated in FIG. 2. As  
12 shown in FIG. 2, the transmitting party T 11 has a plaintext message P 10 to be  
13 transmitted over a non-secure channel 21 to the receiving party R 31. The transmitting  
14 party T 11 uses a transformation generator 13 to generate two transformations  $\alpha$  14 and  $\beta$   
15 15 such that  $\beta$  15 can be reversed, but the combined transformation ( $\alpha$  14) ( $\beta$  15) cannot  
16 be reversed. The transformation  $\alpha$  14 for this example is the creation of a singular (i.e.,  
17 non-invertible) matrix [A] 14 where the plaintext message P 10 is embodied in the upper  
18 left block of the matrix and the remaining three blocks of the matrix are established by  
19 the transformation process to be random or quasi-random elements which exhibit  
20 characteristics such that the matrix [A] 14 cannot be inverted. The second transformation  
21  $\beta$  15 is taken to be that of post-multiplying the matrix [A] 14 by an invertible matrix [B]  
22 15 composed of random or quasi-random elements to create the first encrypted message  
23 [AB] 24. The first encrypted message [AB] 24 which is created by the cryptographic  
24 device 12 is singular or non-invertible because one of its key components – [A] 14  
25 (which embodies P 10) – is singular. The transmitting party T 11 transmits the matrix of  
26 elements in [AB] 24 to the receiving party R 31 over a non-secure channel 21. Upon  
27 receipt of [AB] 24, the receiving party R 31 uses the transformation generator 33 to  
28 generate the transformation  $\gamma$  34 such that  $\gamma$  34 can be reversed. For this example, the  
29 transformation  $\gamma$  34 is taken to be the process of pre-multiplying the matrix [AB] 24 by  
30 an invertible matrix [C] 34 composed of random or quasi-random elements. Once the  
31 cryptographic device 32 is used to apply the transformation  $\gamma$  34 to matrix [AB] 24, the  
32 resulting second encrypted message [CAB] 25 is also singular or non-invertible because  
33 [A] 14, a key component of that result, is singular. The receiving party R 31 transmits  
34 the matrix of elements in [CAB] 25 to the transmitting party T 11 over a non-secure  
35 channel 21. Upon receipt of [CAB] 25, the transmitting party T further transforms  
36 [CAB] 25 by post-multiplying the matrix [CAB] 25 by the inverse of the matrix [B] 15,  
37 which is  $[B]^{-1}$  16. That post-multiplication effectively reverses the transformation  $\beta$  that  
38 was the process of post-multiplying [A] 14 by [B] 15. The resulting third encrypted  
39 message [CA] 26 is also singular or non-invertible because [A] 14 is still a component of  
40 the result and is singular. The transmitting party T 11 transmits the matrix of elements in  
41 [CA] 26 to the receiving party R 31 over a non-secure channel 21. Upon receipt of [CA]  
42 26, the receiving party R 31 further transforms [CA] 26 by pre-multiplying the matrix  
43 [CA] 26 by the inverse of the matrix [C] 34, which is  $[C]^{-1}$  35. That pre-multiplication  
44 effectively reverses the transformation  $\gamma$  34 that was the process of pre-multiplying [AB]  
45 24 by [C] 34. The final result of these combined transformations (implemented in this  
46 example as matrix multiplications) is the matrix [A] 14, which embodies the plaintext



1 message P 10 in its upper left block. That result is now in the possession of the receiving  
2 party R 31. The receiving party R 31 does not know nor need to know the transmitting  
3 party T's 11 transformation matrix [B] 15 nor does the transmitting party T 11 know nor  
4 need to know the receiving party R's 31 transformation matrix [C] 34. Because the  
5 invention doesn't require either party to possess or gain any information about the other's  
6 primary encryption processes, the technique of the invention is designated as an  
7 independent-key process.

8  
9 A specific example of an embodiment of the processes of this invention using the basic  
10 techniques of matrix algebra is shown in FIG. 3. As shown in FIG. 3, the transmitting  
11 party T 11 has a plaintext message P 10 of the phrase "HI" to be transmitted over a non-  
12 secure channel 21 to the receiving party R 31. The phrase "HI" is converted to a numeric  
13 equivalent of "8, 9" using the conversion of "A" to "1", "B" to "2", etc. Other numeric  
14 conversions of characters, such as for the standard ASCII character set, could be used.  
15 The transmitting party T 11 generates two transformations  $\alpha$  14 and  $\beta$  15 such that  $\beta$  15  
16 can be reversed, but the combined transformation ( $\alpha$  14) ( $\beta$  15) cannot be reversed. The  
17 transformation  $\alpha$  14 for this example is taken to be the creation of a singular (i.e., non-  
18 invertible) matrix [A] 14 where the plaintext message P 10 is embodied in the upper left  
19 area of the matrix and the remaining elements of the matrix are established by the  
20 transformation process to be random or quasi-random elements which exhibit  
21 characteristics such that the matrix [A] 14 cannot be inverted. The numeric equivalent  
22 "8, 9" of the message "HI" is loaded in the upper left block of [A] 14 and the remaining  
23 elements are chosen for this example to be "7, 5, 6, 3, 1, 0, 5" so that [A] 14 is non-  
24 invertible. Thus, the transformation  $\alpha$  14 in this example converts the message "HI" to  
25 the non-invertible matrix [A] 14. The second transformation  $\beta$  15 is taken to be that of  
26 post-multiplying the matrix [A] 14 by an invertible matrix [B] 15 composed of random or  
27 quasi-random elements to create the first encrypted message [AB] 24. The matrix [B] 15  
28 is chosen for this example to contain the elements "3, 4, 6, 2, 1, 1, 5, 8, 4" so the  
29 transformation  $\beta$  15 yields the resulting elements of [AB] 24 as "77, 97, 85, 42, 50, 48,  
30 28, 44, 26". This first encrypted message [AB] 24 is singular or non-invertible. The  
31 transmitting party T 11 transmits the matrix of elements in [AB] 24 to the receiving party  
32 R 31 over a non-secure channel 21. Upon receipt of [AB] 24, the receiving party R 31  
33 generates the transformation  $\gamma$  34 such that  $\gamma$  34 can be reversed. For this example, the  
34 transformation  $\gamma$  34 is taken to be the process of pre-multiplying the matrix [AB] 24 by  
35 an invertible matrix [C] 34 composed of random or quasi-random elements. The matrix  
36 [C] 34 is chosen for this example to contain the elements "5, 7, 1, 2, 3, 6, 4, 9, 0" so the  
37 transformation  $\gamma$  34 yields the resulting elements of [CAB] 25 as "707, 879, 787, 448,  
38 608, 470, 686, 838, 772". The resulting second encrypted message [CAB] 25 also is  
39 singular. The receiving party R 31 transmits the matrix of elements in [CAB] 25 to the  
40 transmitting party T 11 over a non-secure channel 21. Upon receipt of [CAB] 25, the  
41 transmitting party T further transforms [CAB] 25 by post-multiplying the matrix [CAB]  
42 25 by the inverse of the matrix [B] 15, which is  $[B]^{-1}$  16. That post-multiplication  
43 effectively reverses the transformation  $\beta$  that was the process of post-multiplying [A] 14  
44 by [B] 15. The resulting third encrypted message [CA] 26 contains the elements "76, 87,  
45 61, 37, 36, 53, 77, 90, 55" and also is singular or non-invertible because [A] 14 is still a  
46 component of the result and is singular. The transmitting party T 11 transmits the matrix

1 of elements in [CA] 26 to the receiving party R 31 over a non-secure channel 21. Upon  
2 receipt of [CA] 26, the receiving party R 31 further transforms [CA] 26 by pre-  
3 multiplying the matrix [CA] 26 by the inverse of the matrix [C] 34, which is  $[C]^{-1}$  35.  
4 That pre-multiplication effectively reverses the transformation  $\gamma$  34 that was the process  
5 of pre-multiplying [AB] 24 by [C] 34. The final result of these combined transformations  
6 (implemented in this example as matrix multiplication) is the original matrix [A] 14 with  
7 the elements "8, 9, 7, 5, 6, 3, 1, 0, 5", which embodies the plaintext message P 10 entered  
8 as "8, 9" in its upper left block. That result is now in the possession of the receiving  
9 party R 31. The receiving party R 31 does not know nor need to know the transmitting  
10 party T's 11 transformation matrix [B] 15 nor does the transmitting party T 11 know nor  
11 need to know the receiving party R's 31 transformation matrix [C] 34 in order for the  
12 plaintext message P 10 to be securely transmitted between the two.

13  
14 The elements of the transformation matrices [B] 15 and [C] 34 and the non-message  
15 elements of the matrix [A] 14 can be considered "key" elements and in conjunction with  
16 the transformation processes could be labeled the "keys" to the cryptographic system of  
17 this invention.

18  
19 Because the cryptographic system of the invention includes a non-secure communications  
20 channel 21, an eavesdropper 41 that is not included in the cryptographic system may  
21 receive all of the communications between the transmitting party T 11 and the receiving  
22 party R 31. The eavesdropper 41 may possess a cryptographic device 42 that includes the  
23 same processing capabilities (matrix multiplication in the case of this example) and  
24 knowledge of the transformation processes (matrix operations in the case of this example)  
25 as the cryptographic devices 12 and 32 available to the transmitting party T 11 and the  
26 receiving party R 31, and a transformation generator 43 that includes the same  
27 capabilities and available transformation processes (matrix operations in the case of this  
28 example) as the transformation generators 13 and 33 available to the transmitting party T  
29 11 and the receiving party R 31. However, even given the full content of the encrypted  
30 messages [AB] 24, [CAB] 25, and [CA] 26, the eavesdropper 41 cannot directly  
31 determine or otherwise deduce the matrices [A] 14, [B] 15, or [C] 34 to determine the  
32 original plaintext message P 10 because the observed matrices [AB] 24, [CAB] 25, and  
33 [CA] 26 are not invertible. The best that the eavesdropper 41 can do with the information  
34 from the messages [AB] 24, [CAB] 25, and [CA] 26 is to establish some limited linear  
35 relationships between some of the elements of the message matrices. However,  
36 knowledge of those linear relationships alone is not very informative or substantially  
37 useful to the eavesdropper 41 since the eavesdropper 41 would still have to guess the  
38 values of many specific elements in the matrices. Refining that linear relationship  
39 information would require an amount of effort by the eavesdropper 41 no less than that  
40 required for a brute-force break of the cryptographic system. Therefore, the  
41 cryptographic system is fully secure, being no more susceptible to cryptanalytic attack  
42 than to a brute-force attack.

43  
44 The precise encrypted messages transmitted 24, 25, 26 between transmitting party T 11  
45 and the receiving party R 31 depend on the plaintext message P 10 and the transformation  
46 processes 14, 15, 34. The options for choices of the transformation processes 14, 15, 34

1 make possible nearly any observable combination of encrypted messages 24, 25, 26  
2 regardless of the initial plaintext message P 10. The magnitude of the alternatives for  
3 observable combinations of encrypted messages is so large as to frustrate any attempt by  
4 an eavesdropper 41 to develop cryptanalytic approaches to attack the cryptographic  
5 system.  
6

7 Although the present invention has been described in terms of the presently preferred  
8 embodiment, it is to be understood that such disclosure is purely illustrative and is not to  
9 be interpreted as limiting. Consequently, without departing from the spirit and scope of  
10 the invention, various alterations, modifications, and/or alternative applications of the  
11 invention will, no doubt, be suggested to those skilled in the art after having read the  
12 preceding disclosure. Accordingly, it is intended that the following claims be interpreted  
13 as encompassing all alterations, modifications, or alternative applications as fall within  
14 the true spirit and scope of the invention.  
15